M'sila University Fcaulty of Mathematics and Computer Department of Mathematics Year 2023/2024

TD Number 2

Exercise 1. Diagonalize the following matrices:

•
$$A = \begin{bmatrix} 2 & 3 & -1 \\ 1 & 0 & -1 \\ 1 & 1 & -2 \end{bmatrix}$$

• $A = \begin{bmatrix} 4 & 1 & 1 & 1 \\ 1 & 4 & 1 & 1 \\ 1 & 1 & 4 & 1 \\ 1 & 1 & 1 & 4 \end{bmatrix}$

Exercise 2.

Find the triangular matrix T similar to A where

•
$$A = \begin{bmatrix} 4 & 3 & 4 \\ 0 & 1 & 0 \\ -1 & -1 & 0 \end{bmatrix}$$

• $A = \begin{bmatrix} 3 & -4 & 0 & 2 \\ 4 & -5 & -2 & 4 \\ 0 & 0 & 3 & -2 \\ 0 & 0 & 2 & -1 \end{bmatrix}$

Exercise 3.

Using the Hamilton-Cayley theorem, find the inverse of the matrix

 $A = \begin{bmatrix} 1 & 0 & -1 \\ 0 & 3 & 1 \\ 0 & 2 & 1 \end{bmatrix}$