

## Tutorial 2

### Exercise 1

Let  $X = [0, 1]$  with  $\alpha, \beta \in \mathbb{R}$  and let  $a, b \in \mathbb{R}$ . Define the fuzzy set  $A$  on  $X$  as follows:

$$\mu_A(x) = \begin{cases} 0, & \text{if } x < a - \alpha \text{ or } b + \beta < x \\ 1, & \text{if } a < x < b \\ 1 + x - \alpha a, & \text{if } a - \alpha < x < a \\ 1 - b - \beta x, & \text{if } b < x < b + \beta \end{cases}$$

Determine  $\text{Ker}(A)$ ,  $\text{Supp}(A)$  and  $H(A)$ .

### Exercise 2

Let  $X = \{1, 2, 3, \dots, 10\}$  and  $A$  a fuzzy subset of  $X$  given by:

$$A = \{ \langle 1, 0.2 \rangle, \langle 2, 0.5 \rangle, \langle 3, 0.8 \rangle, \langle 4, 1.0 \rangle, \langle 5, 0.7 \rangle, \langle 6, 0.3 \rangle, \langle 7, 0.0 \rangle, \langle 8, 0.0 \rangle, \langle 9, 0.0 \rangle, \langle 10, 0.0 \rangle \}$$

Determine all  $\alpha$ -cuts of  $A$ .

### Exercise 3

Let  $A, B$  are two a fuzzy subset on a universe  $X$  and  $\alpha, \beta \in [0, 1]$

- (1) if  $\alpha \leq \beta$ , then  $A_\beta \subseteq A_\alpha$
- (2)  $(A \cap B)_\alpha = A_\alpha \cap B_\alpha$
- (3)  $(A \cup B)_\alpha = A_\alpha \cup B_\alpha$

### Exercise 4

1.  $T_0(x, y) = \begin{cases} 0, & (x, y) \in [0, 1]^2 \\ \min(x, y) & \text{otherwise.} \end{cases}$
2.  $T_1(x, y) = \max(x + y - 1, 0)$ .
3.  $T_{1.5}(x, y) = 2 - x - xyy + xy$ .
4.  $T_2(x, y) = xy$ .
5.  $T_{2.5}(x, y) = x + xyy - xy$ .
6.  $T_3(x, y) = \min(x, y)$ .

Show that we have:  $T_0 \leq T_1 \leq T_{1.5} \leq T_2 \leq T_{2.5} \leq T_3$ .