CHAPTER II: Number Systems

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Number Systems

1. Introduction

Number systems are used to represent and manipulate numerical data in computer systems. Commonly used number systems include the decimal (base-10), binary (base-2), octal (base-8), and hexadecimal (base-16) systems[6]⁶.

2. Polynomial Form

& Définition :

Polynomial form is a method for representing numbers in computer systems. It involves expressing a number as a polynomial with coefficients multiplied by powers of the base[6]⁶.

To watch the video click here¹

3. Decimal Value of a Base-b Number (BD)

& Définition :

The decimal value of a base-b number can be calculated using the polynomial form. Each digit in the number is multiplied by the corresponding power of the base and then summed [5]⁵.

Equation:

$$D_b=d_n imes b^n+d_{n-1} imes b^{n-1}+...+d_1 imes b^1+d_0 imes b^0$$

QExemple :

Convert the binary number 10111011 to its decimal equivalent[4]⁴.

$$D_{10} = 1 imes 2^3 + 0 imes 2^2 + 1 imes 2^1 + 1 imes 2$$
 $D_{10} = 8 + 0 + 2 + 1 = 11$

4. Base Conversion

∞Définition :

Base conversion involves converting numbers from one base to another. Common conversions include binary-to-decimal, decimal-to-binary, binary-to-octal, octal-to-binary, binary-to-hexadecimal, and hexadecimal-to-binary[5]⁵.

4.1. Converting a Decimal Number to a Base-b Number (BD)

\$[‡] Méthode :

To convert a decimal number to a base-b number, repeatedly divide the decimal number by the base and record the remainders. The base-b number is then formed by arranging the remainders in reverse order $[4]^4$.

4.2. Binary-Octal (BO) and Vice Versa Conversion

*S*Fondamental :

Binary and octal are both base-2 and base-8 number systems, respectively. Converting between binary and octal involves grouping binary digits into sets of three and replacing each set with its corresponding octal digit [6]⁶.

4.3. Binary-Hexadecimal (BH) and Vice Versa Conversion

*S***Fondamental** :

Binary and hexadecimal are both base-2 and base-16 number systems, respectively. Converting between binary and hexadecimal involves grouping binary digits into sets of four and replacing each set with its corresponding hexadecimal digit[4]⁴.

5. Complementation

&Définition :

Complementation is a technique used in computing to represent negative numbers and perform arithmetic operations. There are two main methods of complementation: one's complement and two's complement[5]⁵.

5.1. Signed Encoding (SE)

\$*Méthode :

Signed encoding is a method of representing positive and negative numbers using a sign bit. In signed encoding, the leftmost bit (most significant bit) of a binary number represents the sign, where 0 indicates a positive number and 1 indicates a negative number/ 61^6 .

*Q*Exemple :

In a signed 8-bit encoding, the binary number 01010101 represents the positive decimal number 85, while 11010101 represents the negative decimal number -43.

5.2. One's Complement (OC)

©^{*}Méthode :

One's complement is a method of representing negative numbers by taking the bitwise complement (reversing all bits) of the binary representation of a positive number. In one's complement, negative numbers are denoted by setting the sign bit to $1[5]^5$.

*Q*Exemple :

To find the one's complement of 010101010, we simply flip all the bits to get 10101011, which represents -85.

5.3. Two's Complement (TC)

✿^{*}Méthode :

Two's complement is a method of representing negative numbers by taking the one's complement of the binary representation of a positive number and adding 1. In two's complement, negative numbers are denoted by setting the sign bit to 1 and using the standard binary addition operation $[4]^4$.

*Q*Exemple :

To find the two's complement of 01010101, we first find the one's complement to get 101010101, then add 1 to get 101010111, which represents $-85[4]^4$.

Number Systems