

Physics 01: Mechanics of point particle.

University Year 2024-2025

Series N° 01: Mathematical background

EXERCISE 01:

1- Which of the following quantities are vector or scalar quantities?

(a) Velocity (b) Displacement (c) Kinetic Energy (d) Momentum (e) Acceleration (f) Work (g) Weight (h) Power.

EXERCISE 02:

1- What are the dimensions of the following quantities?

- Velocity ($\mathbf{v}$), Acceleration ($\mathbf{a}$), Force ($\mathbf{F}$), Density (ρ , which is mass per unit volume), Pressure ($\mathbf{P}$, which is force per unit area).

2- For a fluid with constant density ρ , the velocity $\mathbf{v}$, pressure $\mathbf{P}$ and height $\mathbf{h}$ are related by Bernoulli's equation:

$$P + \frac{1}{2} \rho v^2 + \rho g h = \text{Constant}$$

g is the acceleration due to gravity.

Show that the left side of the Bernoulli's equation is dimensionally consistent.

3- Use dimensional analysis to determine which of the following equation is certainly wrong?

$$\lambda = vt, \quad F = \frac{m}{a}, \quad F = \frac{mv}{t}, \quad h = \frac{v^2}{2g} \quad (\lambda \text{ and } h \text{ are lengths})$$

EXERCISE 03 (home work):

The speed of sound, v , in a gas might plausibly depend on the pressure, p , the density, ρ , and the volume, V , of the gas. Use dimensional analysis to determine the formula of v

EXERCISE 04:

1- The magnitude of the centripetal force F_c acting on an object is a function of mass m of the object, its velocity v , and the radius r of the circular path. By the method of dimensional analysis, find an expression for the centripetal force.

2- The frequency of vibration f of a mass m at the end of spring that has a stiffness constant k is related to m and k by a relation of the form $f = (\text{constant})m^a k^b$.

Use dimensional analysis to find a and b . it is known that $[f] = [T]^{-1}$ and $[k] = [M][T]^{-2}$.

EXERCISE 05:

1- Newton's law of universal gravitation is given by $F_G = G \frac{m_1 m_2}{r^2}$, where F_G is the force of attraction of one mass m_1 upon another mass m_2 at a distance r . Find the SI units of the constant G .

2- Find the exponents n and m in the formula : $x = \frac{1}{2} a^n t^m$

Where x : distance, a : acceleration and t : time.

EXERCISE 06:

1- Represent the following points in the Cartesian referential: $M_1(3,1, -2)$, $M_2(1,2,1)$, $M_3(-3, 2, 1)$, $M_4(-1,1,2)$ and find the vectors $\vec{A} = \overrightarrow{M_1 M_2}$ and $\vec{B} = \overrightarrow{M_3 M_4}$

2- Calculate: (a) $\vec{A} + \vec{B}$, (b) $\vec{A} - \vec{B}$, (c) $\|\vec{A}\|$, $\|\vec{B}\|$, (d) $(\vec{A} + \vec{B})^2$, (e) $A^2 + B^2$, (f) $\vec{A} \cdot \vec{B}$, (g) the angle between $\vec{A}$ and $\vec{B}$, (h) $\vec{A} \wedge \vec{B}$, (i) the directional cosines of $\vec{A}$ and $\vec{B}$, (j) the unit vector of $\vec{A}$ and $\vec{B}$.

3- Given the vector $\vec{C} = x\vec{i} + y\vec{j} + z\vec{k}$; find x and z for each case: (a) $\vec{C}$ parallel to $\vec{A}$, (b) $\vec{C}$ is perpendicular to $(\vec{A}$ and $\vec{B})$ at the same time.

EXERCISE 07 (home work):

Relative to a fixed origin O , the respective position of three points A , B and C are:

$$A(3,2, 9), \quad B(-5,11,6), \quad C(4, 0, -8)$$

1- Determine, in component form, the vectors $\overrightarrow{AB}$ and $\overrightarrow{AC}$

2- Find the angle $\hat{BAC}$.

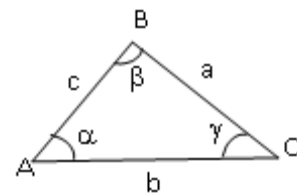
3- Calculate the area of the triangle BAC .

EXERCISE 08:

1- By using the properties of the vector product, show that the following equation is satisfied in triangle ABC (see figure 1): $\frac{a}{\sin \alpha} = \frac{b}{\sin \beta} = \frac{c}{\sin \gamma}$

2- Prove that:

$$\cos \alpha = \frac{b^2 + c^2 - a^2}{2bc}$$



EXERCISE 09:

1- Given $\vec{A} = 3t\vec{i} - (t^2 + t)\vec{j} + (t^3 - 2t^2)\vec{k}$. Calculate $\frac{d\vec{A}(t)}{dt}$ and $\frac{d^2\vec{A}(t)}{dt^2}$. Apply for $t=2$ s.

2- Given $\vec{B} = e^{-wt}\vec{i} + \sin wt\vec{j} + \cos wt\vec{k}$ (w is constant). Calculate $\frac{d\vec{B}(t)}{dt}$ and $\frac{d^2\vec{B}(t)}{dt^2}$