



Robotique industrielle

Master I Fabrication mécanique et productive

Par : Dr. Slamani Mohamed

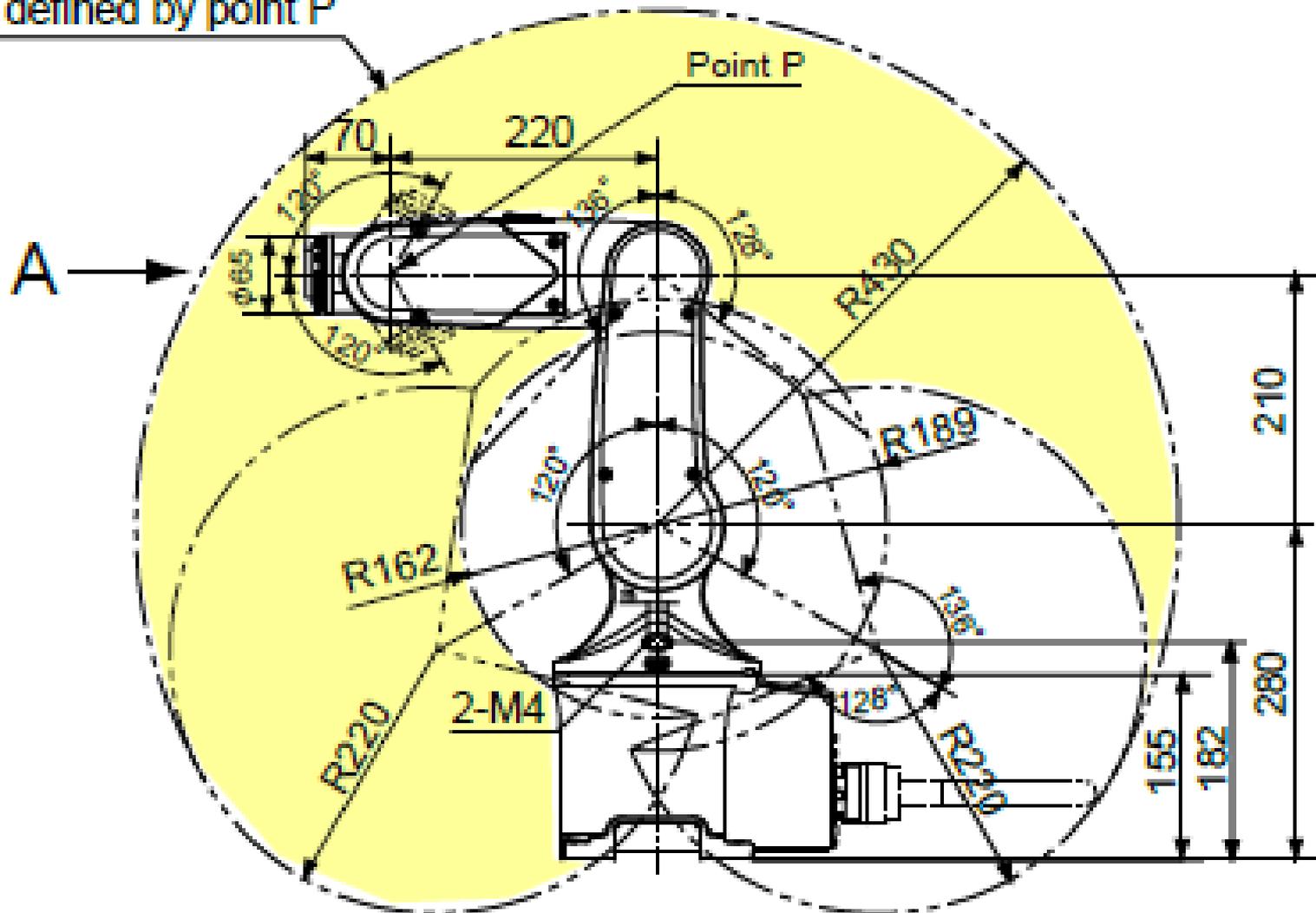
1985

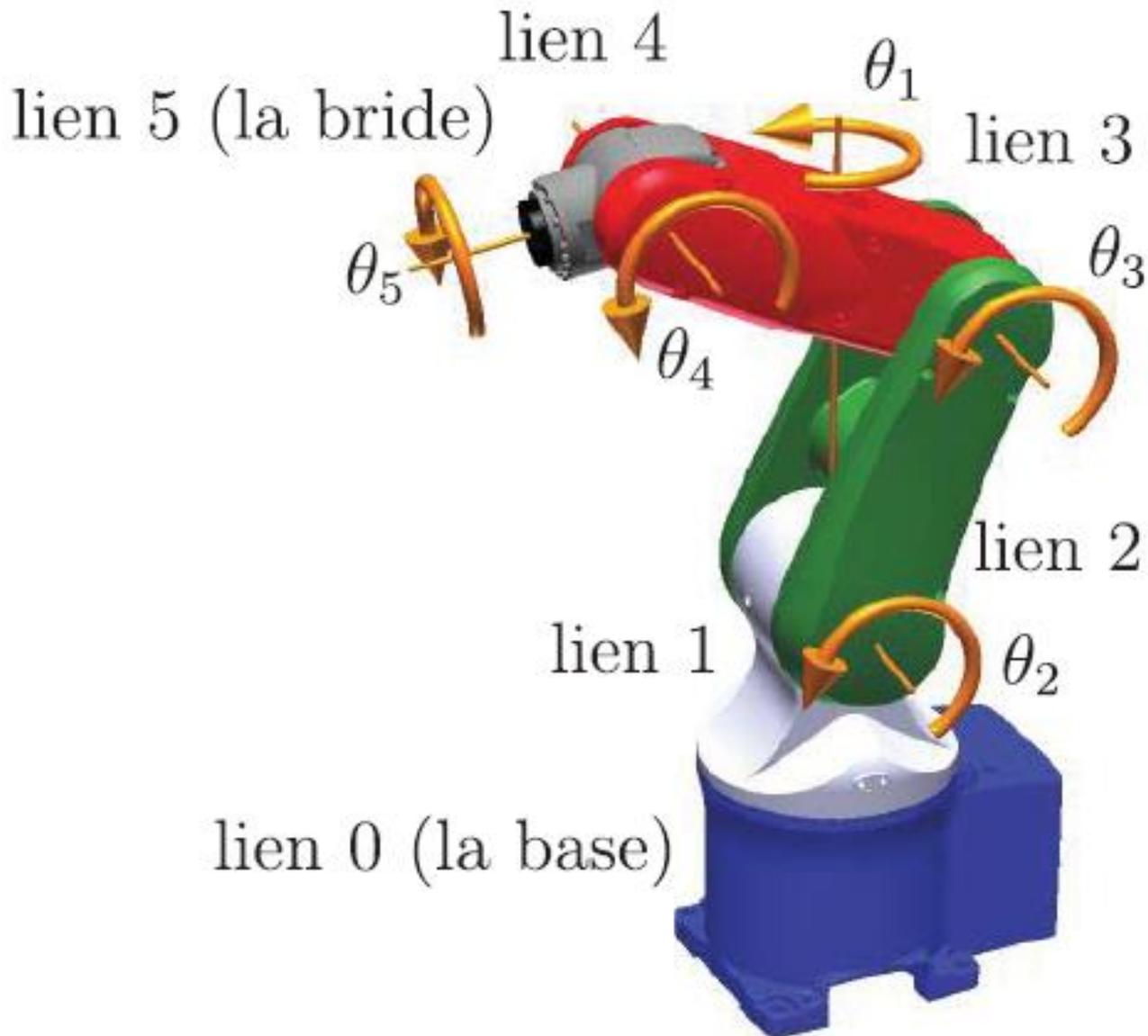


Cinématique directe

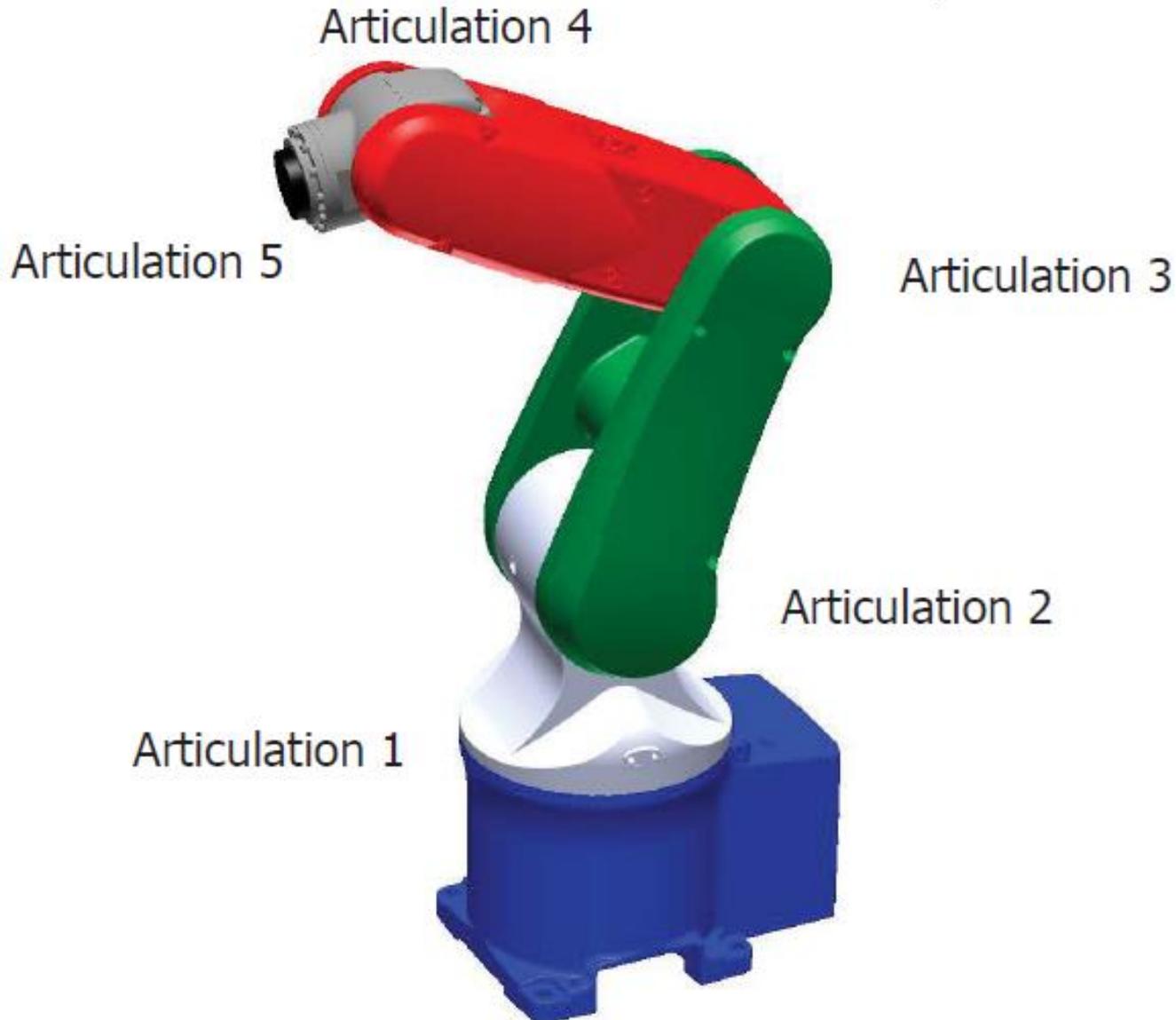
Exemple d'un robot sériel a cinq articulations rotoïdes

Workable space
defined by point P

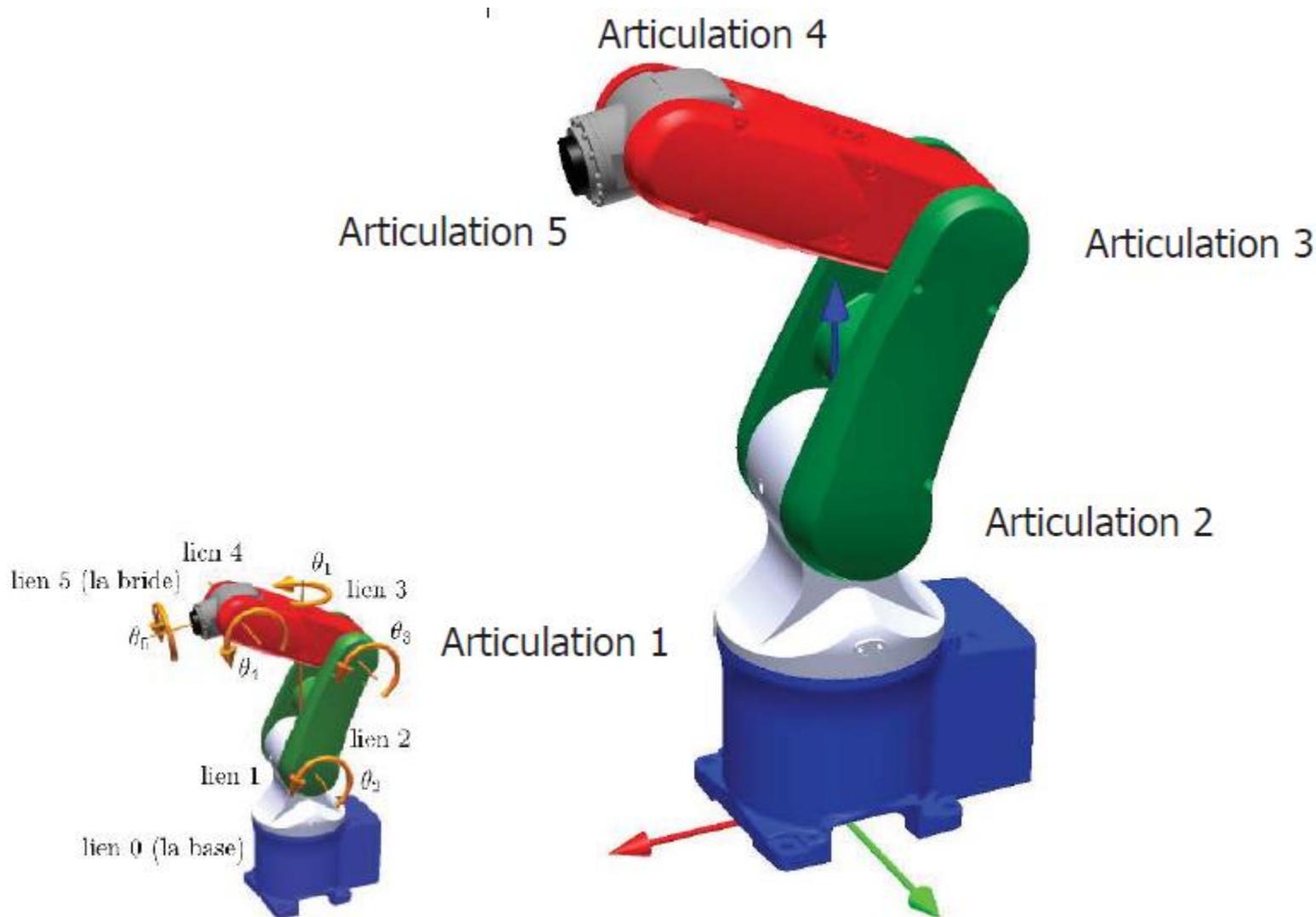




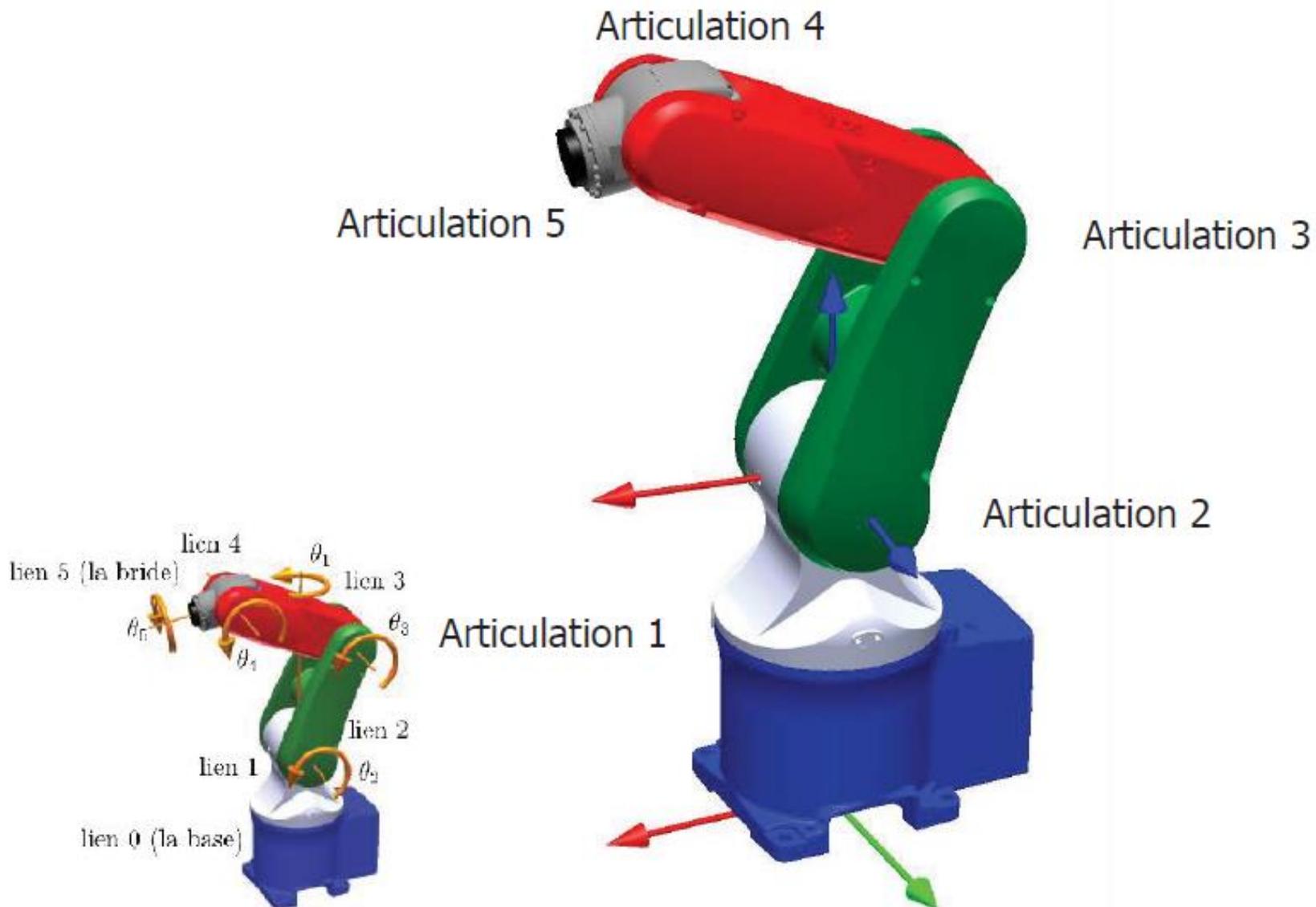
Placer les référentiels DH



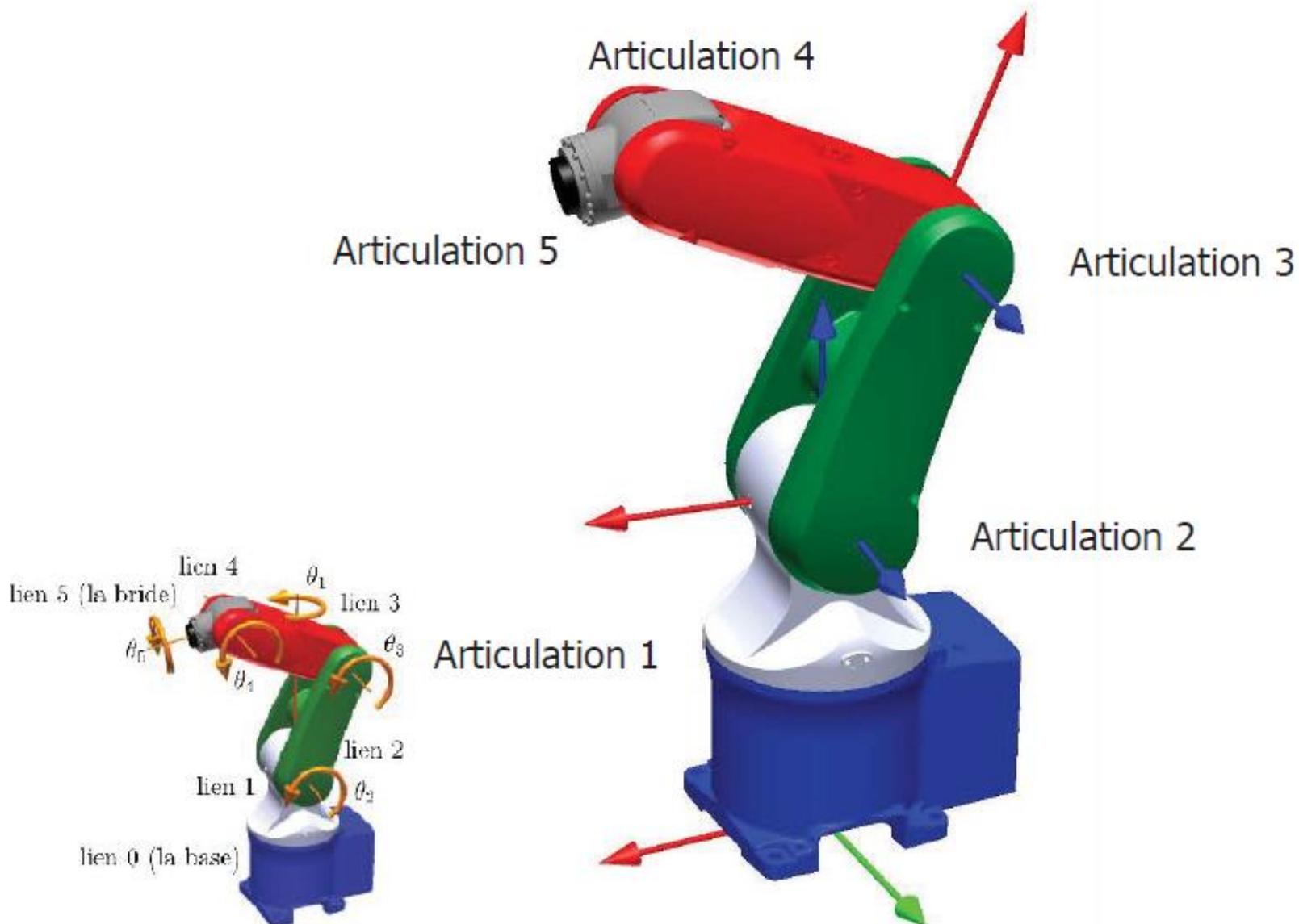
Référentiel F_0



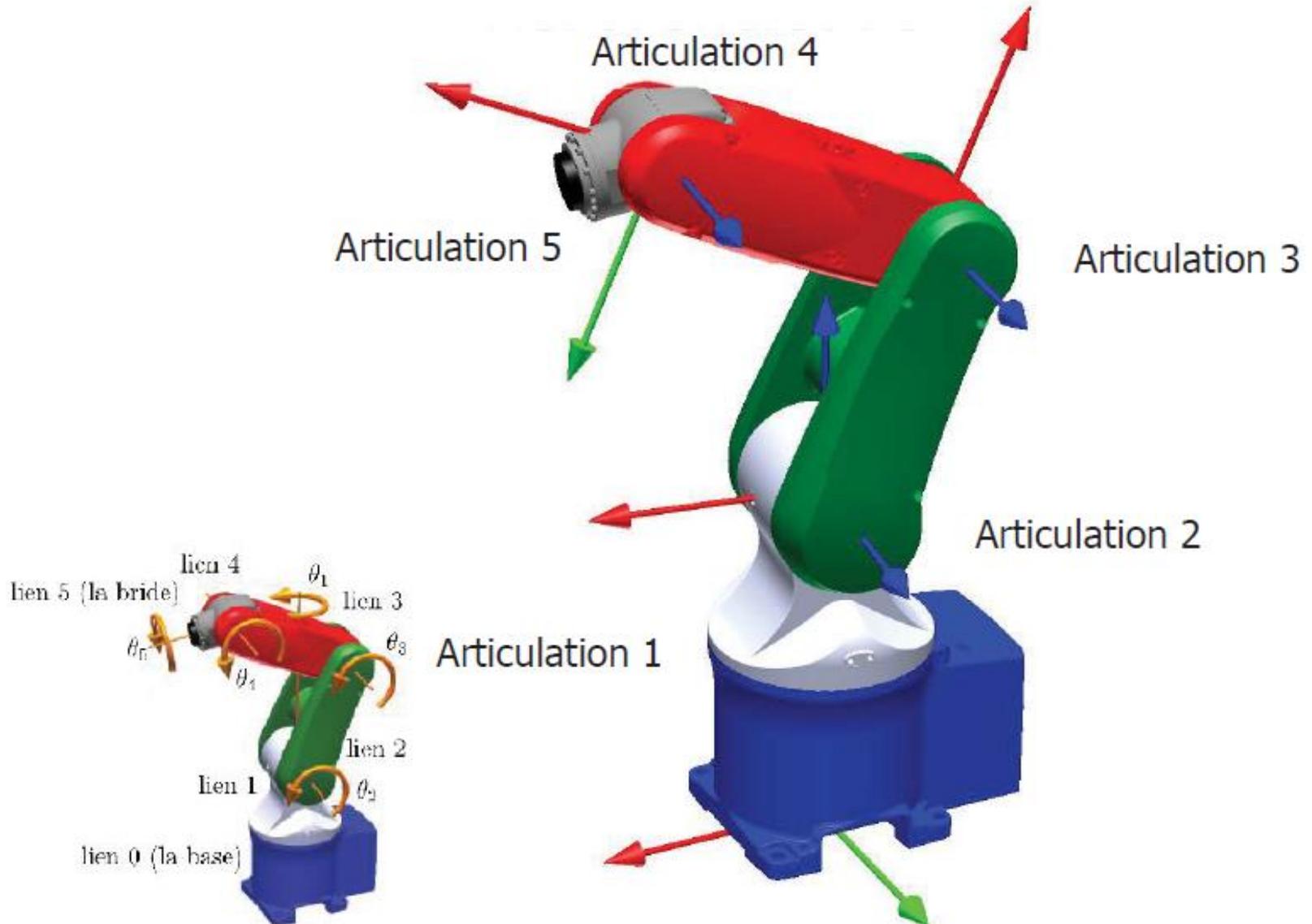
Référentiel F1

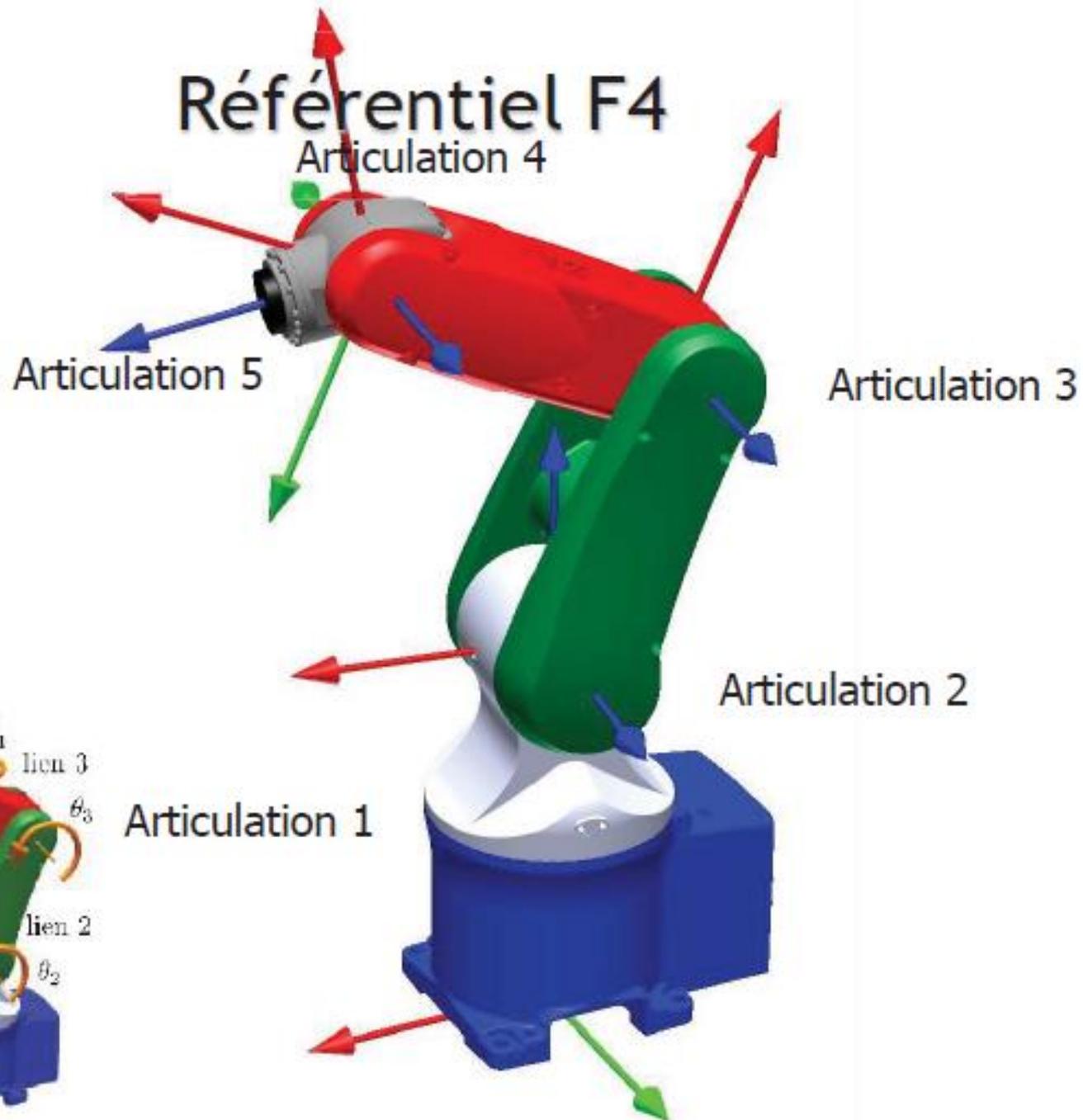
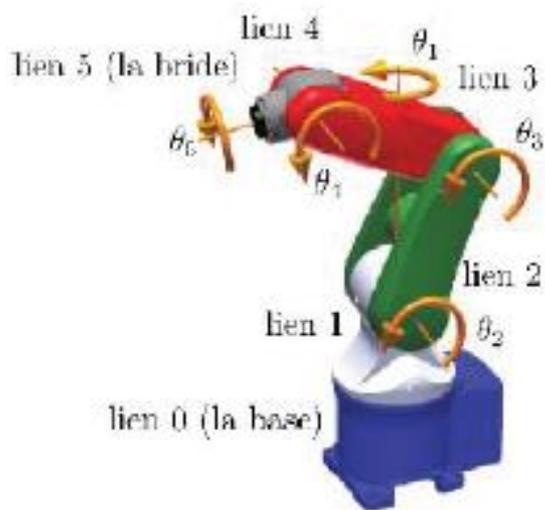


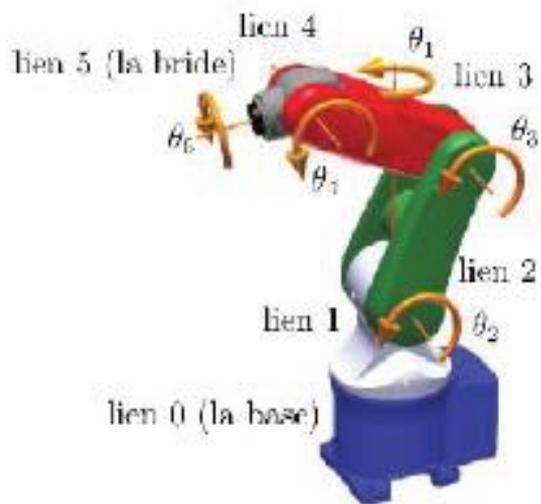
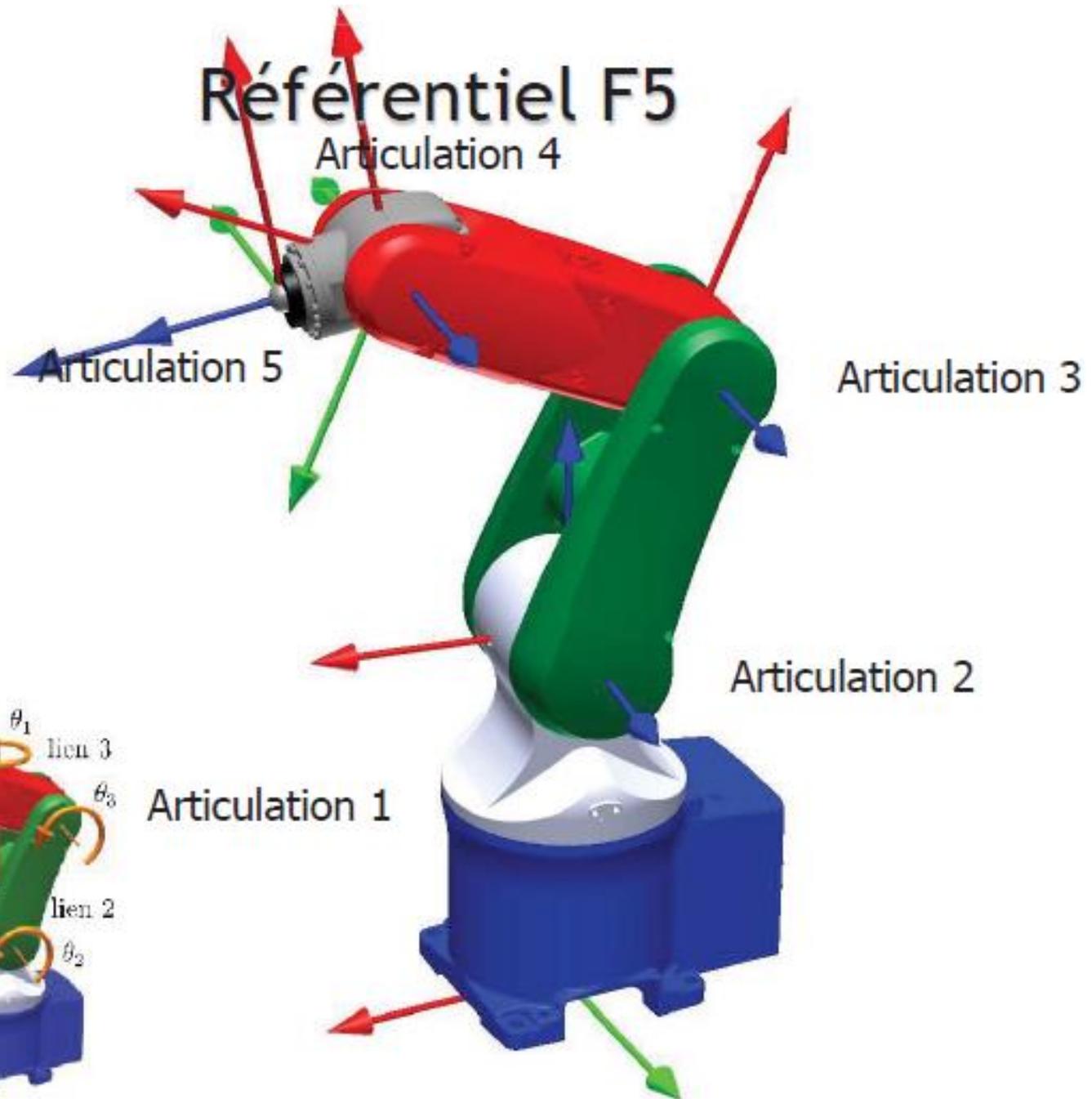
Référentiel F2



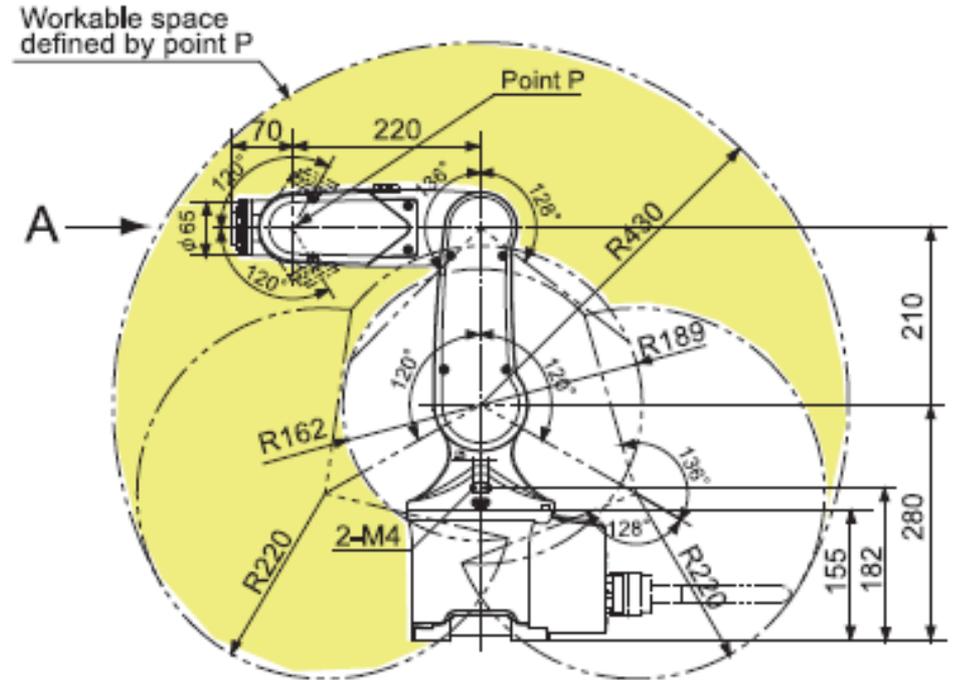
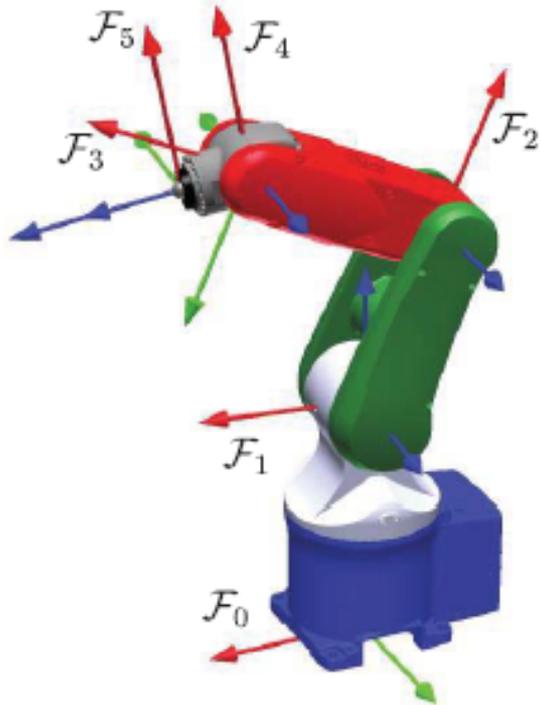
Référentiel F3







Paramètres DH conformes avec le robot réel



i	θ_i	d_i	a_i	α_i
1	θ_1	280 mm	0 mm	-90°
2	$\theta_2 - 90^\circ$	0 mm	210 mm	0°
3	θ_3	0 mm	220 mm	0°
4	$\theta_4 - 90^\circ$	0 mm	0 mm	-90°
5	θ_5	70 mm	0 mm	0°

$$\begin{aligned} \mathbf{H}_1^0 &= \mathbf{H}_{rot,z}(\theta_1)\mathbf{H}_{trans}(0, 0, 280)\mathbf{H}_{trans}(0, 0, 0)\mathbf{H}_{rot,x}(-90^\circ) \\ &= \begin{bmatrix} \cos \theta_1 & 0 & -\sin \theta_1 & 0 \\ \sin \theta_1 & 0 & \cos \theta_1 & 0 \\ 0 & -1 & 0 & 280 \\ 0 & 0 & 0 & 1 \end{bmatrix}, \end{aligned}$$

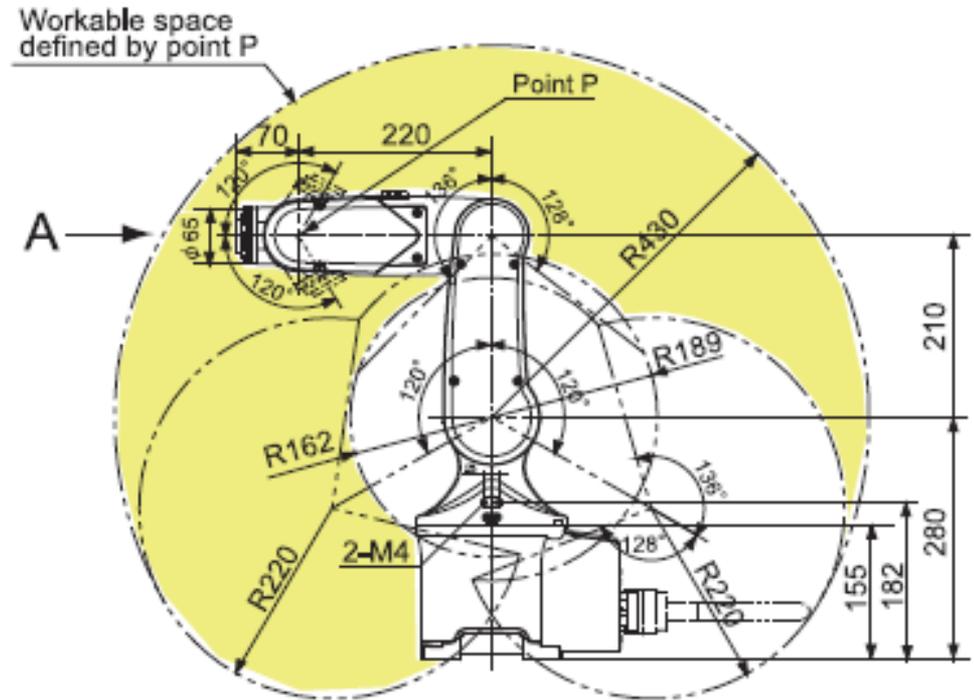
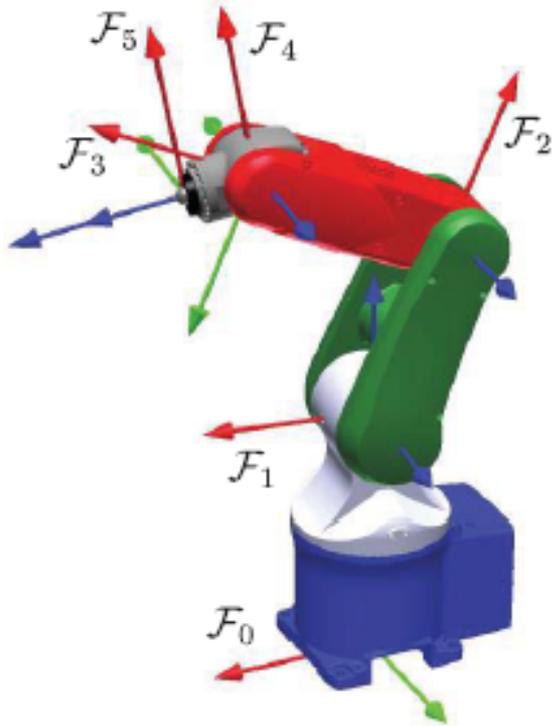
$$\begin{aligned} \mathbf{H}_2^1 &= \mathbf{H}_{rot,z}(\theta_2 - 90^\circ)\mathbf{H}_{trans}(0, 0, 0)\mathbf{H}_{trans}(210, 0, 0)\mathbf{H}_{rot,x}(0^\circ) \\ &= \begin{bmatrix} \sin \theta_2 & \cos \theta_2 & 0 & 210 \sin \theta_2 \\ -\cos \theta_2 & \sin \theta_2 & 0 & -210 \cos \theta_2 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}, \end{aligned}$$

$$\begin{aligned} \mathbf{H}_3^2 &= \mathbf{H}_{rot,z}(\theta_3)\mathbf{H}_{trans}(0, 0, 0)\mathbf{H}_{trans}(220, 0, 0)\mathbf{H}_{rot,x}(0^\circ) \\ &= \begin{bmatrix} \cos \theta_3 & -\sin \theta_3 & 0 & 220 \cos \theta_3 \\ \sin \theta_3 & \cos \theta_3 & 0 & 220 \sin \theta_3 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}, \end{aligned}$$

$$\begin{aligned} \mathbf{H}_4^3 &= \mathbf{H}_{rot,z}(\theta_4 - 90^\circ)\mathbf{H}_{trans}(0, 0, 0)\mathbf{H}_{trans}(0, 0, 0)\mathbf{H}_{rot,x}(-90^\circ) \\ &= \begin{bmatrix} \sin \theta_4 & 0 & \cos \theta_4 & 0 \\ -\cos \theta_4 & 0 & \sin \theta_4 & 0 \\ 0 & -1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}, \end{aligned}$$

$$\begin{aligned} \mathbf{H}_5^4 &= \mathbf{H}_{rot,z}(\theta_5)\mathbf{H}_{trans}(0, 0, 70)\mathbf{H}_{trans}(0, 0, 0)\mathbf{H}_{rot,x}(0^\circ) \\ &= \begin{bmatrix} \cos \theta_5 & -\sin \theta_5 & 0 & 0 \\ \sin \theta_5 & \cos \theta_5 & 0 & 0 \\ 0 & 0 & 1 & 70 \\ 0 & 0 & 0 & 1 \end{bmatrix}. \end{aligned}$$

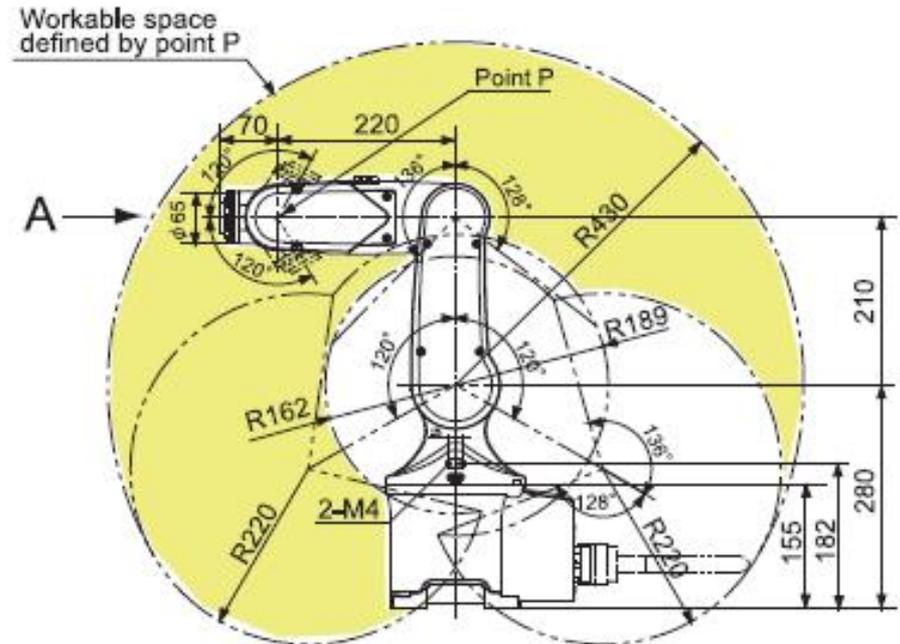
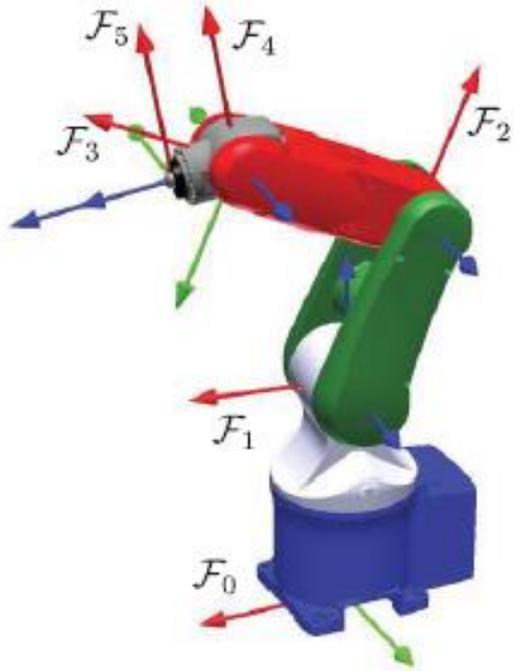
Équation de la cinématique directe



$$H_5^0 = H_1^0 H_2^1 H_3^2 H_4^3 H_5^4$$

$$= \begin{bmatrix} -c_1 c_{234} c_5 + s_1 s_5 & c_1 c_{234} s_5 + s_1 c_5 & c_1 s_{234} & c_1 (70 s_{234} + 220 s_{23} + 210 s_2) \\ -s_1 c_{234} c_5 - c_1 s_5 & s_1 c_{234} s_5 - c_1 c_5 & s_1 s_{234} & s_1 (70 s_{234} + 220 s_{23} + 210 s_2) \\ s_{234} c_5 & -s_{234} s_5 & c_{234} & 280 + 70 c_{234} + 220 c_{23} + 210 c_2 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

Validation dans la configuration zéro



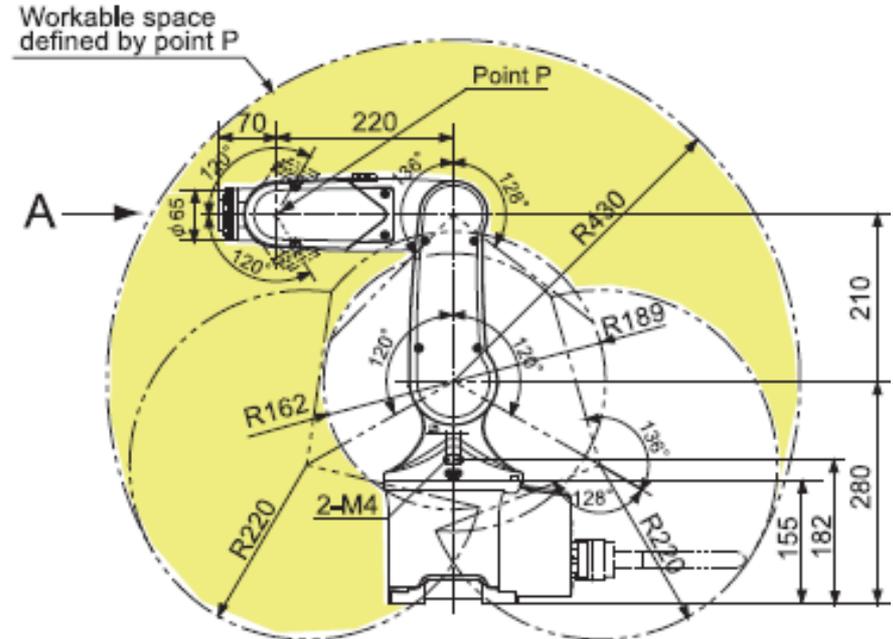
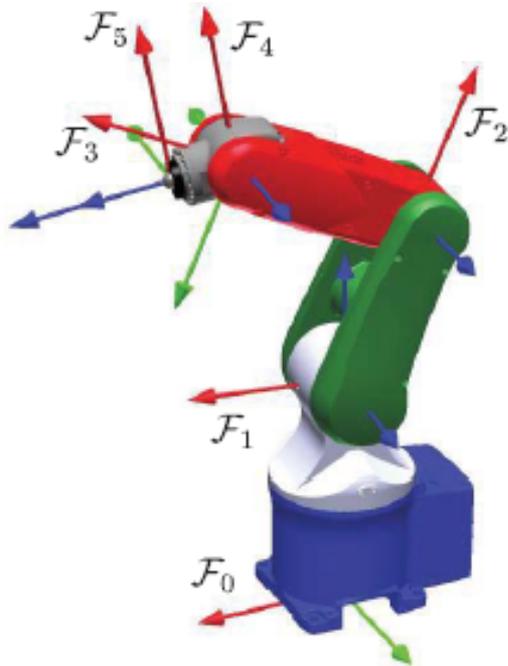
$$\theta_1 = 0^\circ, \theta_2 = 0^\circ, \theta_3 = 0^\circ, \theta_4 = 0^\circ, \theta_5 = 0^\circ \longrightarrow$$

$$\mathbf{H}_5^0 = \begin{bmatrix} -1 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 \\ 0 & 0 & 1 & 780 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$\mathbf{H}_5^0 = \mathbf{H}_1^0 \mathbf{H}_2^1 \mathbf{H}_3^2 \mathbf{H}_4^3 \mathbf{H}_5^4$$

$$= \begin{bmatrix} -c_1 c_{234} c_5 + s_1 s_5 & c_1 c_{234} s_5 + s_1 c_5 & c_1 s_{234} & c_1 (70 s_{234} + 220 s_{23} + 210 s_2) \\ -s_1 c_{234} c_5 - c_1 s_5 & s_1 c_{234} s_5 - c_1 c_5 & s_1 s_{234} & s_1 (70 s_{234} + 220 s_{23} + 210 s_2) \\ s_{234} c_5 & -s_{234} s_5 & c_{234} & 280 + 70 c_{234} + 220 c_{23} + 210 c_2 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

Validation dans une autre configuration



$$\theta_1 = 0^\circ, \theta_2 = 0^\circ, \theta_3 = 90^\circ, \theta_4 = 0^\circ, \theta_5 = 0^\circ \longrightarrow$$

$$\mathbf{H}_5^0 = \begin{bmatrix} 0 & 0 & 1 & 290 \\ 0 & -1 & 0 & 0 \\ 1 & 0 & 0 & 490 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$\mathbf{H}_5^0 = \mathbf{H}_1^0 \mathbf{H}_2^1 \mathbf{H}_3^2 \mathbf{H}_4^3 \mathbf{H}_5^4$$

$$= \begin{bmatrix} -c_1 c_{234} c_5 + s_1 s_5 & c_1 c_{234} s_5 + s_1 c_5 & c_1 s_{234} & c_1 (70 s_{234} + 220 s_{23} + 210 s_2) \\ -s_1 c_{234} c_5 - c_1 s_5 & s_1 c_{234} s_5 - c_1 c_5 & s_1 s_{234} & s_1 (70 s_{234} + 220 s_{23} + 210 s_2) \\ s_{234} c_5 & -s_{234} s_5 & c_{234} & 280 + 70 c_{234} + 220 c_{23} + 210 c_2 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$