

Physics 01: Mechanics of point particle.

University Year 2023-2024

Tutorial N° 05 Practice: Work and Energy

EXERCISE 01

The constant forces $\vec{F}_1 = \vec{i} + 2\vec{j} + 3\vec{k}$ N and $\vec{F}_2 = 4\vec{i} - 5\vec{j} - 2\vec{k}$ N act together on a particle during a displacement from position $\vec{r}_2 = 7\vec{k}$ cm to position $\vec{r}_1 = 20\vec{i} + 15\vec{j}$ cm.

- Determine the total work done on the particle.

EXERCISE 02

The potential energy of an object is given by $E_p(x) = 5x^2 - 4x^3$ where E_p is in joules and x is in metres.

- a- What is the force, $\vec{F}(x)$, acting on the object?
- b- Determine the positions where the object is in equilibrium and state whether they are stable or unstable.

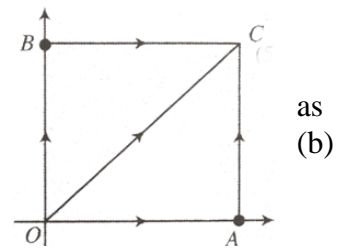
EXERCISE 03

A 40 kg box initially at rest is pushed 5 m along a rough horizontal floor with a constant applied horizontal force of 130 N. The coefficient of friction between the box and floor is 0.3. Find:

- 1- The work done by the applied force,
- 2- The energy lost due to friction,
- 3- The change in kinetic energy of the box,
- 4- The final velocity of the box.

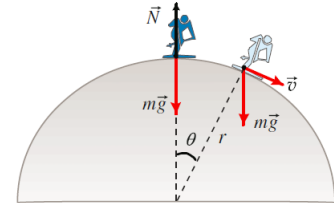
EXERCISE 04

A particle moves in x-y plane in figure under the influence of a friction force with magnitude 3 N. Calculate the work done by the friction force on particle it moves along the following closed paths: (a) path OA and return path AO, path OA followed by AC and the return path CO, (c) path OC followed by the return path CO (OA= OB= 5 m). What do you conclude?



EXERCISE 05

A skier of mass m starts sliding from rest at the top of a solid frictionless hemisphere of radius r . At what angle θ will the skier leave the sphere?



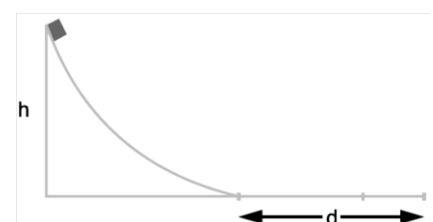
EXERCISE 06

A steel ball of mass $m=5$ g is projected vertically downward from a height $h=14.8$ m with an initial speed $V_0=10$ m/s. The ball penetrates itself in sand to a depth $d=20$ cm. Neglect air resistance and take g to be 10 m/s².

- 1- Calculate the velocity of the ball when it reaches the surface of the sand?
- 2- What is the magnitude of the average force exerted by the sand on the ball?

EXERCISE 07

A ramp in an amusement park is frictionless. A smooth object slides down the ramp and comes down through a height h , (Figure). What distance d is necessary to stop the object on the flat track if the coefficient of friction is μ .



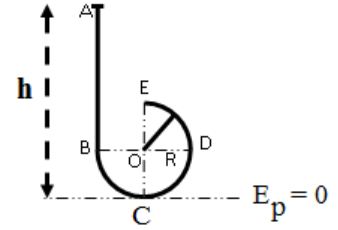
EXERCISE 08

A ball of mass m is released from a height H without initial velocity. AB is a vertical surface and $BCDE$ is a $\frac{3}{4}$ of a circle of radius R .

1- The ball moves without friction:

- a- calculate the velocity of the ball at point B.
- b- calculate the velocity of the ball at point C.
- c- For what value of h does the ball reaches the point E with a velocity $\sqrt{2gR}$.

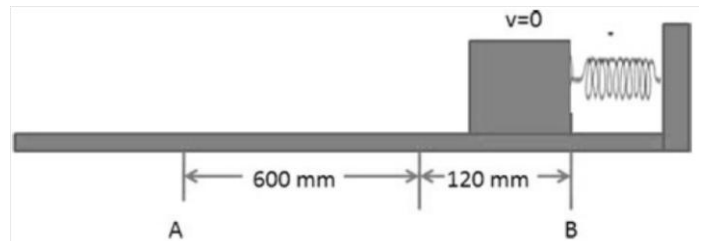
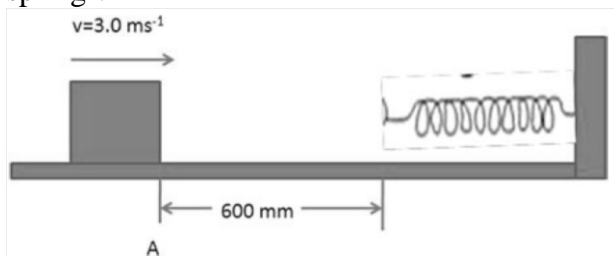
2- Assuming that the motion takes place with a constant tangential friction force F_f in the $BCDE$ part only. What is the value of F_f if the ball just reaches point E (the velocity at point E is zero).



EXERCISE 09

A spring is used to stop a crate of mass 50 kg which is sliding on a horizontal surface. The spring has a spring constant $k = 20\text{ kN/m}$ and is initially in its equilibrium state. In position A shown in the top diagram the crate has a velocity of 3.0 m/s . The compression of the spring when the crate is instantaneously at rest (position B in the bottom diagram) is 120 mm .

- (a) What is the work done by the spring as the crate is brought to a stop?
- (b) Write an expression for the work done by friction during the stopping of the crate (in terms of the coefficient of kinetic friction).
- (c) Determine the coefficient of friction between the crate and the surface.
- (d) What will be the velocity of the crate as it passes again through position A after rebounding off the spring ?



F. Mezahi, S. Hamrit